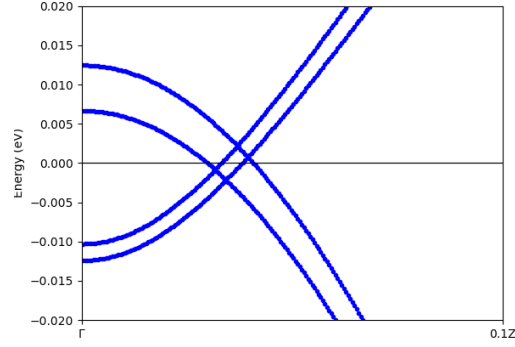
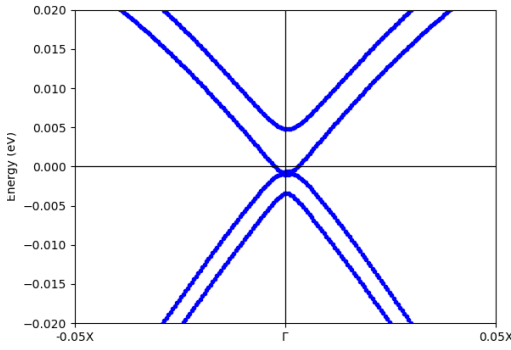


**Supplemental Material:**  
**Co-emergence of Dirac and multi-Weyl Topological Excitations**  
**in Pnictide Antiperovskites**

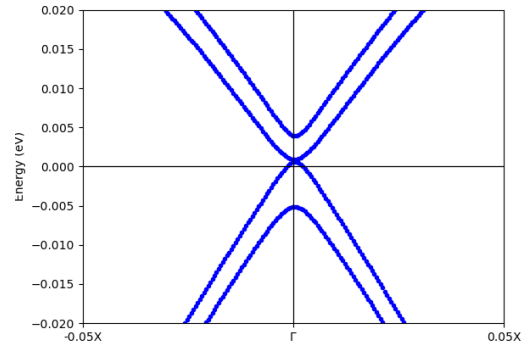
Wen Fong Goh and Warren E. Pickett  
*Department of Physics, University of California, Davis CA 95616, USA*  
(Dated: May 8, 2018)

**EXPLICIT VIEW OF MULTI-WEYL CHARACTER**

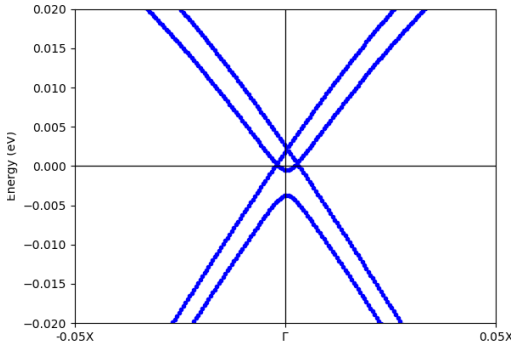
A set of hopping amplitudes was obtained from Wannier functions based on 48 atomic orbitals, viz. Bi  $6p$ , P  $3p$ , Ca  $4s, 3d$ . The 4 bands crossings along  $\Gamma$ -Z as shown in Fig. 1a are reproduced by hopping amplitudes extending to nine neighbour unit cells. Fig. 1b-1e show energy dispersion *perpendicular* to  $\hat{z}$  for each of the four degenerate points, where two are seen to be multi-Weyls (Fig. 1b and 1c), *i.e.* dispersion is linear along  $\hat{z}$  but quadratic in directions perpendicular to  $\hat{z}$ . This behavior is also seen in other Dirac semimetals, eg. Na<sub>3</sub>Bi. The tight binding scheme can be extended to obtain a  $4 \times 4$  model Hamiltonian through  $k \cdot p$  expansion at  $\Gamma$  point. However, since the Weyl points do not occur at small  $k$ , such an abbreviated expansion cannot reproduce a reliable description for the band crossings.

(a) Band crossings along  $\Gamma$ -Z

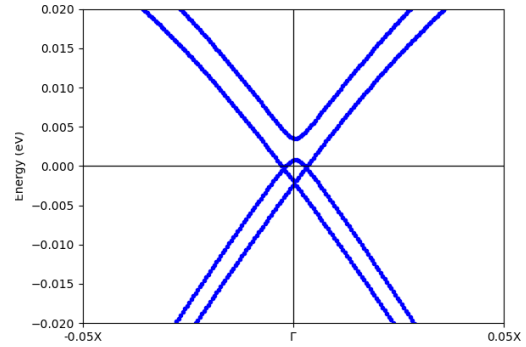
(b) Left point



(c) Right point



(d) Top point



(e) Bottom point

FIG. 1: Band structures obtained from the hopping-parameters up to nine neighbouring cells (six is minimum number of cells for the resulting bands to be reasonable). (a) The energy bands along  $\Gamma$ -Z shows four degenerate points where two are multi-Weyl points. (b)-(e) Energy dispersion perpendicular to  $\hat{z}$  at  $k_{z,j} = 0.032$  (left point),  $0.039$  (right point),  $0.037$  (bottom point) and  $0.034$  (top point), in units of  $(\frac{\pi}{c})$ .